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# Barriers to Rotation and Inversion in meso-1, $1^{\prime}-\mathrm{Bi}(2-m e t h y l p i p e r i d i n e){ }^{1}$ 

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#### Abstract

A ${ }^{13} \mathrm{C}$ DNMR study of meso-1,1-bi(2-methylpiperidine) (7), meso-1, $1^{\prime}$-bi(cis-2,4-dimethylpiperidine) (8), and meso-1,1'-bi(cis-4-tert-butyl-2-methylpiperidine) (9) with the aid of molecular mechanics calculation of the corresponding hydrocarbons $1,1^{\prime}$-bi(2-methylcyclohexane) (14), 1, $1^{\prime}$-bi(cis-2,4-dimethylcyclohexane) (15), and 1,1'-bi(cis-4-tert-butyl-2methylcyclohexane) (16) is reported. The most stable conformations of the bipiperidines are the enantiomeric conformations in which the lone pairs of the nitrogen atoms are approximately gauche to each other. In these conformations the $\mathrm{N}-\mathrm{N}$ bond and all of the alkyl groups are equatorial to each of the chair-form piperidine rings. The energy barriers ( $\Delta G^{*}$ ) to the interconversion between these enantiomeric gauche conformations in 7,8 , and 9 are $12.5\left(-25^{\circ} \mathrm{C}\right), 17.7\left(+72^{\circ} \mathrm{C}\right)$, and $19.0 \mathrm{kcal}^{\mathrm{mol}}{ }^{-1}(+97$ ${ }^{\circ} \mathrm{C}$ ), respectively. While the barrier for 7 is assigned to the passing inversion of the nitrogen atoms, the barriers for $\mathbf{8}$ and 9 are assigned to the single-passing rotation about the $\mathrm{N}-\mathrm{N}$ bond. In the case of 7 , the next stable conformations, in which one of the methyl groups is axial, were observed at the lower temperatures. The free energy difference between the next stable and the most stable conformations is $0.55 \mathrm{kcal} \mathrm{mol}^{-1}$ at $-117^{\circ} \mathrm{C}$, and the energy barrier between these conformations is 9.2 kcal $\mathrm{mol}^{-1}$ at $-82^{\circ} \mathrm{C}$, which is assigned to the ring inversion.


## Introduction

Conformational analysis of hydrazines has attracted the interest of physical and organic chemists for more than three decades. ${ }^{2}$ Its static aspects have been investigated extensively. It is established that in a simple acyclic alkylhydrazine both of the nitrogen atoms are pyramidal and that in the most stable conformation of such a hydrazine the lone pairs are gauche to each other. ${ }^{3-5}$ Its dynamic aspects, however, still lack the elucidation of fundamental problems, one of which is concerned with the energy barrier to nitrogen inversions and that to rotations about the $\mathrm{N}-\mathrm{N}$ bond. ${ }^{2,6}$
Jones, Katritzky, and co-workers have discovered that there are two types of nitrogen inversions, a passing N -inversion (an inversion that involves eclipsing of one pair of substituents in the transition state) and a nonpassing N -inversion (an inversion that does not involve eclipsing of substituents). ${ }^{7}$ The high energy

[^0]barrier in 1,2-dimethylperhydropyridazines ( $\Delta G^{*} \simeq 12 \mathrm{kcal}$ $\left.\mathrm{mol}^{-1}\right)^{8}$ has been interpreted in terms of the passing N -inversion, and the low energy barrier in 1,2-dimethylperhydropyridazines ${ }^{8}$ and acyclic alkylhydrazines 1,2 , and $3\left(\Delta G^{*} \simeq 7-8 \mathrm{kcal} \mathrm{mol}^{-1}\right)^{9}$


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has been interpreted in terms of the nonpassing N -inversions. ${ }^{7}$ Originally this barrier difference was attributed to the presence or absence of the alkyl substituents passing. Later Nelsen and Weisman pointed out that the barrier difference should be attributed to the difference in the magnitude of the interaction of the lone pairs in the transition state between the two N -inversions. ${ }^{10}$ While in the transition state of a passing N -inversion two lone pairs are approximately parallel to each other causing a large repulsive interaction which results in a high barrier; in the transition state of a nonpassing N -inversion, two lone pairs are approximately orthogonal to each other resulting in a low barrier (see Figure 1).
Shvo classified the rotation about the $\mathrm{N}-\mathrm{N}$ bond into two types, a single-passing rotation (a rotation that involves eclipsing of only

[^1]

Figure 1. Diagram contrasting lone-pair-lone-pair interactions for the passing (high barrier) and for the nonpassing nitrogen inversion (low barrier), in hydrazine ABN-NCD.


Figure 2. Partial diagram for the conformational interconversion in hydrazine ABN-NCD. A light, a broken, and a dotted arrow represent a nonpassing N -inversion, a passing N -inversion, and a single-passing rotation, respectively.
one pair of substituents in the transition state) and a double-passing rotation (a rotation that involves eclipsing of two pairs of substituents). ${ }^{11}$ While in the transition state of a double-passing rotation a passing of lone pairs occurs, in a single-passing rotation a passing of lone pairs does not occur. It is expected that the barrier to a double-passing rotation should be substantially higher than that to a single-passing rotation. This expectation has been supported by an infrared and a microwave spectroscopic study of methylhydrazine ${ }^{12}$ and theoretical studies. ${ }^{13}$ Rotational barriers of bipyramidal hydrazines other than methylhydrazine have never been determined unambiguously.

Fletcher and Sutherland found the free energy barriers of $10.7-11.2 \mathrm{kcal} \mathrm{mol}^{-1}$ for the conformational interconversion in tetraalkylhydrazines 4,5 , and 6 by ${ }^{1} \mathrm{H}$ NMR. They assigned these

$$
\begin{aligned}
& \underset{R^{1}-\mathrm{N}-\mathrm{N}^{-}-\mathrm{RH}_{2}^{2}}{ } \\
& 4: R^{1}=R^{2}=E t \\
& \text { 5: } R^{1}=R^{2}=\text { iso- } \mathrm{Pr} \\
& \text { 6: } \mathrm{R}^{1}=\mathrm{CH}_{2} \mathrm{Ph}, \mathrm{R}^{2}=\mathrm{Et}
\end{aligned}
$$

barriers to the "rotation" about the $\mathrm{N}-\mathrm{N}$ bond. ${ }^{14}$ Jones, Katritzky, and co-workers ${ }^{7}$ and Shvo, ${ }^{2}$ however, have pointed out that the reported barriers can be accounted for by assigning them to the passing N -inversion, as well as by assigning them to the singlepassing rotation. The two alternative processes have hitherto never been differentiated in acyclic hydrazines in solution. The difficulty in the differentiation between the two alternatives is that they can

[^2]Table 1. ${ }^{13} \mathrm{C}$ NMR Spectra of cis- (10) and trans-4-tert-Butylpiperidine (11) in $\mathrm{CDCl}_{3}$

| position | 10 |  |  | $T_{1} / \mathrm{s}$ | 11 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\delta_{\text {obsd }}$ | $\delta_{\text {calcd }}$ |  |  | $\delta_{\text {obsd }}$ | $\delta^{\text {calcd }}$ |  |
| 2 | 52.61 | 53.0 | d | 4.1 | 47.46 | 46.9 | d |
| 3 | 35.86 | 35.8 | t | 2.5 | 32.20 | 32.9 |  |
| 4 | 46.94 | 46.6 |  | 4.2 | $(40.07)^{\text {b }}$ | 40.6 |  |
| 5 | 27.11 | 27.2 |  | 2.3 | 28.11 | 28.1 |  |
| 6 | 47.22 | 47.8 |  | 2.4 | $(40.20)^{6}$ | 41.0 |  |
| $2-\mathrm{CH}_{3}$ | 23.18 |  | q | 2.3 | 17.92 |  | q |
| $\mathrm{C}\left(\mathrm{CH}_{3}\right)_{3}$ | 32.26 |  | s | 17.3 | 32.14 |  |  |
| $\mathrm{C}\left(\mathrm{CH}_{3}\right)_{3}$ | 27.34 |  |  | 2.1 | 27.20 |  | q |

${ }^{a}$ Multiplicity determined by off-resonance decoupling. ${ }^{b}$ Assignments may be exchanged.
bring about the same net conformational interconversion through the same trans conformation (see Figure 2).

We describe here the first successful differentiation between the two alternatives in meso-1, $1^{\prime}$ - bi (2-methylpiperidine) (7), meso-1, $1^{\prime}$-bi(cis-2,4-dimethylpiperidine) (8), and meso- $1,1^{\prime}$-bi-(cis-4-tert-butyl-2-methylpiperidine) (9), which leads to the estimation of the barrier to the single-passing rotation, with the aid of ${ }^{13} \mathrm{C}$ DNMR of these compounds and of molecular mechanics calculations of the corresponding hydrocarbons.

Synthesis of Materials. Synthesis of 7 has already been reported. ${ }^{15}$ The bipiperidines 8 and 9 were prepared by the sil-ver(I)-catalyzed peroxodisulfate oxidation of the corresponding piperidines (see eq 1). Preparation of cis-4-tert-butyl-2-

methylpiperidine (10) was accomplished by catalytic hydrogen-



ation of 4-tert-butyl-2-methylpyridine (12), which was prepared by methylation of 4-tert-butylpyridine with methyllithium.
${ }^{13} \mathrm{C}$ NMR Spectra of cis- (10) and trans-4-tert-Butyl-2methylpiperidine (11). ${ }^{13} \mathrm{C}$ NMR spectra of 10 and 11 , the latter being the byproduct in the catalytic hydrogenation of 12, are summarized in Table I. Calculated chemical shifts of $\mathbf{1 0}$ and 11 were obtained for the 2 -methyl equatorial conformation and the 2-methyl axial conformation, respectively, using the parameters of Eliel et al. for methylpiperidines. ${ }^{16}$ Effects of the equatorial tert-butyl group to the chemical shifts of the ring carbon, which was not included in parameters of Eliel et al. or of Booth et al., ${ }^{17}$ were estimated by comparison of chemical shifts of tert-butylcyclohexane ( $\delta 48.4(\mathrm{C} 1), 27.7(\mathrm{C} 2), 27.3(\mathrm{C} 3), 26.7(\mathrm{C} 4)^{18}$ with the chemical shift of cyclohexane ( $\delta 26.9$ ); ${ }^{19}$ the tert-butyl group
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Table II. ${ }^{13} \mathrm{C}$ NMR Data for meso-1, 1 '- $\mathrm{Bi}(2$-methylpiperidine)s


[^3] cal shft in parentheses. See the text. ${ }^{d}$ Signal intensities are classified as strong (s) and weak (w). Peaks $s$ and $w$ correspond to those for $G-S R$ eeee ( $\mathrm{G}+S R$ eeee) and $\mathrm{G}+S$ Seeea ( $\mathrm{G}-R R$ eaee), respectively. ${ }^{e}$ The signal still collapsed into the base line. $f$ Relative assignments uncertain. ${ }^{\boldsymbol{g}}$ The signal was not detected. ${ }^{h}$ The signal did not split. ${ }^{i} T_{1}$ measurements were unsuccessful.


Figure 3. Variable-temperature ${ }^{13} \mathrm{C}$ NMR spectra of meso-1,1'-bi(2methylpiperidine) (7): (i) in diglyme- $d_{14}$; (ii-iv) in THF- $d_{8} / \mathrm{CS}_{2}=5 / 6$.
causes downfield shift of $21.5,0.8,0.4$, and -0.2 ppm at $\alpha, \beta, \gamma$, and $\delta$ positions, respectively. Thus, for 10,

$$
\begin{aligned}
\delta(\mathrm{C} 2) & =47.61+5.04+0.4=53.05 \\
\delta(\mathrm{C} 3) & =27.37+7.72+0.8=35.89 \\
\delta(\mathrm{C} 4) & =25.30-0.11+21.5=46.69 \\
\delta(\mathrm{C} 5) & =27.37-0.92+0.8=27.25 \\
\delta(\mathrm{C} 6) & =47.61-0.15+0.4=47.86
\end{aligned}
$$

Chemical shifts of 11 were calculated in a similar fashion. Agreement of the observed and the calculated chemical shifts is fairly good (within $\pm 0.8 \mathrm{ppm}$ ). The peaks for C2, C3, C5, $2-\mathrm{Me}$,


Figure 4. Variable-temperature ${ }^{13} \mathrm{C}$ NMR spectra of meso-1, $1^{\prime}$-bi(cis-2,4-dimethylpiperidine) (8) in diglyme- $d_{14}$.
and $\mathrm{CMe}_{3}$ in 10 and the peaks for $\mathrm{C} 2, \mathrm{C} 5,2-\mathrm{Me}$, and $\mathrm{CMe}_{3}$ in 11 were assigned from the calculated data, the off-resonance spectra, and/or the signal intensities. Assignment of the peaks for C4 and C6 in 10, which overlapped each other, was based on the spin-lattice relaxation times $T_{1}$, which were measured by the inversion recovery method; ${ }^{20}$ the methine carbon C 4 ( $T_{1}, 4.2 \mathrm{~s}$ ) and the methylene carbon C6 ( $T_{1}, 2.4 \mathrm{~s}$ ) were clearly differentiated. The peaks for C 3 and $\mathrm{CMe}_{3}$ in 11 were assigned in a similar manner. Thus, on the basis of the analysis of the ${ }^{13} \mathrm{C}$ NMR spectra, the configurations and conformations of 10 and 11 were established.
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a:-




Figure 5. All of the typical gauche and trans conformations in meso-1, $1^{\prime}$-bi(2-methylpiperidine) (7), meso-1, $1^{\prime}$-bi(cis-2,4-dimethylpiperidine) (8), and meso-1, $1^{\prime}$-bi(cis-4-tert-butyl-2-methylpiperidine) (9). Symbol 2-e (2-a) in the Newman projections indicates that the 2 -methyl group is equatorial (axial). Symbols $2^{\prime}$-e and $2^{\prime}$-a have analogous meanings for the $2^{\prime}$-methyl group. Symbol e (a) written on a lone pair indicates that the lone pair is equatorial (axial). Heavy lines connecting each of the conformations represent inversions of the piperidine rings.

Variable-Temperature ${ }^{13} \mathrm{C}$ NMR of 7,8 , and 9 . The ${ }^{13} \mathrm{C}$ NMR spectra of the three bipiperidines at various temperatures are summarized in Table II. All of the peaks except for those of the methyl carbons of the tert-butyl groups split into two peaks of equal intensity as the temperature was lowered (see Figures 3 and 4). For 7, below $-45^{\circ} \mathrm{C}$ each of the equally split peaks further splits into two peaks with intensity ratio of ca. 85:15 (see Figure 3). Arguments for the assignment of the signals will appear in later section.
The activation parameters for the rate process were calculated by the total-line-shape analysis (TLS) as well as by the coalescence temperature ( $T_{\mathrm{c}}$ ) method. ${ }^{21}$ They are summarized in Table III. The agreement between $\Delta G^{*}{ }_{\mathrm{c}}$ values calculated by TLS and those by the $T_{\mathrm{c}}$ method for a rate process is good. Activation parameters obtained from different peaks in one compound agree well.

## Discussion

Nomenclature of Conformations. In the bipiperidines the nitrogen inversion (the passing and the nonpassing N -inversion), the rotation about the $\mathrm{N}-\mathrm{N}$ bond (the single-passing and the double-passing rotation), and the ring inversion operate. All of the typical gauche and trans conformations which are interconvertible by these processes are depicted in Figure 5. We designate conformations in Figure 5 as follows. The first descriptor indicates whether the lone pairs are gauche ( G ) or trans ( T ) to each other. The second descriptor represents the sign of the torsion angle of the $\mathrm{N}-\mathrm{N}$ bond with respect to the lone pairs. We designate these two descriptors as the torsion descriptors. The third and the fourth

[^4]descriptors represent the configurations of the nitrogen atoms N1 and $\mathrm{Nl}^{\prime}$, respectively. We designate these two descriptors as the configuration descriptors. The fifth descriptor indicates whether the $\mathrm{N}-\mathrm{N}$ bond is equatorial (e) or axial (a) to the front ring in the Newman projection (ring A). The sixth descriptor indicates whether the 2-methyl group is equatorial (e) or axial (a) to ring A. The seventh descriptor indicates whether the $\mathrm{N}-\mathrm{N}$ bond is equatorial (e) or axial (a) to the rear ring in the Newman projection (ring B). The last descriptor indicates whether the $2^{\prime}$ methyl group is equatorial (e) or axial (a) to ring B. We designate the last four descriptors as the ring conformation descriptors.
The Most Stable Conformations of 7, 8, and 9. It is established that in the most stable conformation of $1,1^{\prime}$-bipiperidine the lone pair electrons of the nitrogen atoms are approximately gauche to each other (the torsion angle $\simeq 90^{\circ}$ ) with the $\mathrm{N}-\mathrm{N}$ bond equatorial to each of the chair-form piperidine rings. ${ }^{3}$ Hence, the most stable conformation of the bipiperidines 7, 8, and 9 are certainly the enantiomeric gauche conformations designated as $\mathrm{G}-S R$ eeee and $\mathrm{G}+$ SReeee, in which the $\mathrm{N}-\mathrm{N}$ bond and all of the alkyl groups are equatorial to each of the piperidine rings, as shown in Figure 5. When the interconversion between the two conformations is fast on the time scale of NMR, the two piperidine units are equivalent and the bipiperidines have an apparent $C_{2}$ symmetry. When the interconversion becomes slow, the apparent $C_{2}$ symmetry disappears and the signal splittings with the intensity ratio of $1: 1$ occur. Calculated chemical shifts for G-SReeee ( $\mathrm{G}+S$ Reeee) in 7 and 8 are consistent with the observed chemical shifts (see later section). Hence, the observed rate processes for 7 over $-45^{\circ} \mathrm{C}$ and for 8 and 9 correspond to the interconversion between G-SReeee and G $+S R$ eeee.
Conformational Diagram. In the conformational diagram (Figure 6), each of the conformations is placed at corners of the


Figure 6. Conformational diagram for meso-1, $1^{\prime}$-bi(2-methylpiperidine) (7), meso-1, $1^{\prime}$-bi (cis-2,4-dimethylpiperidine) (8), and meso-1,1'-bi(cis-4-tert-butyl-2-methylpiperidine) (9). A light, a broken, and a heavy line represent a nonpassing nitrogen inversion, a passing nitrogen inversion, and a ring inversion, respectively. Red spots represent the sterically possible conformations in 7 and $\mathbf{8}$, and red lines represent the lowest barrier inversion paths in these compounds; green spots represent the sterically possible conformation in 9 , and green lines represent the lowest barrier inversion path in this compound.
squares. Each of the squares is designated in terms of the torsion and the configuration descriptors. Conformations on each of the squares are interconvertible by ring inversions, for which the torsion and the configuration descriptors are invariant. An inversion of ring A causes changes of the first two of the ring conformation descriptors. An inversion of ring $B$ causes changes of the last two of the ring conformation descriptors.

Horizontal lines connecting corners of the different squares represent nonpassing N -inversions. Dotted lines connecting corners of different squares represent passing N -inversions. A nonpassing N -inversion causes an interconversion from G to G , and a passing N -inversion causes an interconversion from G to T or from T to G. A nitrogen inversion (passing or nonpassing) of N 1 changes the first one of the ring conformation descriptors, and a nitrogen inversion of $\mathrm{N} 1^{\prime}$ changes the third one of the ring conformation descriptors.

Rotational processes are not depicted in the diagram to avoid complication. They can be represented by connecting corners having the same configuration and ring conformation descriptors. Thus the corresponding corners of the following squares are
connected by single-passing rotations: $\mathrm{G}-S R, \mathrm{~T} \pm S R, \mathrm{G}+S R$; $\mathrm{G}+S S, \mathrm{~T} \pm S S, \mathrm{G}-S S ; \mathrm{G}-R S, \mathrm{~T} \pm R S, \mathrm{G}+R S ; \mathrm{G}+R R, \mathrm{~T} \pm R R, \mathrm{G}-R R$. Double-passing rotations are given by the following connections: $\mathrm{G}-S R, \mathrm{G}+S R ; \mathrm{G}+S S, \mathrm{G}-S S ; \mathrm{G}-R S, \mathrm{G}+R S ; \mathrm{G}+R R, \mathrm{G}-R R$.

Rotating Newman projections of the gauche conformations in the bottom series by $180^{\circ}$ with respect to the axis that bisects the $\mathrm{N}-\mathrm{N}$ bond orthogonally, we can understand that each of the 16 gauche conformations in the top series has a corresponding enantiomeric gauche conformation in the bottom series. Enantiomeric relationships exist between the same numbered corners of $\mathrm{G}-S R$ and $\mathrm{G}+S R$, between those of $G+S S$ and $\mathrm{G}-R R$, between those of $\mathrm{G}-R S$ and $\mathrm{G}+R S$, and between those of $\mathrm{G}+R R$ and $G-S S$. For example, the enantiomer of $G-S R$ aaee is $G+S R$ eeaa.

Our task is to find the lowest barrier path for the interconversion between $\mathrm{G}-S$ Reeee and $\mathrm{G}+S$ Reeee. As stated in the Introduction, the double-passing rotation cannot be involved in the lowest barrier path. Hence, the double-passing rotation is excluded from consideration. As a result, one of the trans conformations must be involved in the interconversion between the two enantiomeric gauche conformations.
Table 11I. Activation Parameters for Conformational Process in meso $\cdot 1,1^{\prime} \cdot \operatorname{Bi}(2-$ methylpiperidine $) s$

| compd | signal | line-shape analysis |  |  |  | coalescence-temp analysis |  |  |  | assignment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | temp range ${ }^{\text {a }}$ | $\Delta H^{\ddagger} b$ | $\Delta S^{\ddagger} \boldsymbol{c}$ | $\Delta G^{\ddagger}{ }_{298}{ }^{\text {d }}$ | $\Delta \nu / \mathrm{Hz}$ | $T{ }^{\prime}{ }^{\circ} \mathrm{C}$ | $\Delta G^{\ddagger}{ }^{\ddagger}{ }^{\text {d }}$ | $\Delta G^{\ddagger} \mathbf{c}^{\boldsymbol{d}, \boldsymbol{e}}$ |  |
| $7{ }^{\text {f }}$ | $\mathrm{C} 2,2^{\prime}$ | -45 to 15 | $11.86 \pm 0.24$ | $-2.93 \pm 0.96$ | $12.74 \pm 0.05$ | 40.0 | -18 |  | $12.60 \pm 0.00$ | $\mathrm{G}-\mathrm{SR}$ eeee $\rightleftharpoons \mathrm{G}+$ SReeee |
|  | $\mathrm{C} 3,3^{\prime}$ |  |  |  |  | $3.9$ | $-40$ | $12.52 \pm 0.10$ |  | GSReec ${ }^{\text {F G SReeee }}$ |
|  | C5,5' | -45 to -1 | $11.80 \pm 0.43$ | $-3.14 \pm 1.74$ | $12.67 \pm 0.1$ | 18.6 | -25 | $12.60 \pm 0.05$ | $12.52 \pm 0.00$ |  |
|  | C4,4' |  |  |  |  | 11.2 | -29 | $12.62 \pm 0.07$ | $12.52 \pm 0.00$ |  |
|  | $2.2{ }^{\prime} \cdot \mathrm{Me}$ | -41 to 25 | $11.70 \pm 0.22$ | $-3.60 \pm 0.81$ | $12.76 \pm 0.02$ | 75.2 | -10 | $12.64 \pm 0.05$ | $12.64 \pm 0.00$ |  |
|  | 2-Me | -106 to -55 | $7.07 \pm 0.56$ | $-9.84 \pm 3.13$ | $9.90 \pm 0.34$ | 210.0 | $\sim-82$ |  | $9.20 \pm 0.00$ | $\mathrm{G}-\mathrm{S} R$ eeee $\rightleftharpoons \mathrm{G}+S S$ eeea and $\mathrm{G}+S R$ eeee $\rightleftharpoons \mathrm{G}-R R$ eaee |
|  | C6 | -106 to -59 | $6.86 \pm 0.79$ | $-11.28 \pm 4.11$ | $10.23 \pm 0.45$ | 105.5 | $\sim-90$ |  | $8.92 \pm 0.02$ | G-SReee $\rightleftharpoons$ G+SSceca and G+SRece $\rightleftharpoons$-R-RReaee |
| $8^{g}$ | C3,3' |  |  |  |  | 9.3 | 62 | $17.66 \pm 0.07$ |  | G-SR eeee $\rightleftharpoons \mathrm{G}+$ SReeee |
|  | C5.5' | $31 \text { to } 103$ | $17.10 \pm 0.62$ | $-1.77 \pm 1.82$ | $17.64 \pm 0.07$ | 20.5 | 72 | $17.69 \pm 0.05$ | $17.71 \pm 0.01$ | GSReee $\rightleftharpoons$ G+SRecee |
|  | C4,4' | 31 to 103 | $17.17 \pm 0.67$ | $-1.57 \pm 1.98$ | $1.98 \pm 0.10$ | 19.5 | 71 | $17.66 \pm 0.05$ | $17.76 \pm 0.01$ |  |
| $9^{g}$ | $\mathrm{C} 4,4^{\prime}$ | 48 to 145 | $17.53 \pm 0.45$ | $-4.03 \pm 1.24$ | $18.74 \pm 0.07$ | 19.0 | 97 | $19.07 \pm 0.07$ | $19.03 \pm 0.01$ | G-SRecee $\rightleftharpoons \mathrm{G}+$ SReeee |
|  | C3, ${ }^{\prime}$ | $48 \text { to } 95$ | $17.84 \pm 0.67$ | $-3.09 \pm 1.94$ | $18.76 \pm 0.10$ | 7.3 | 80 | $18.83 \pm 0.10$ | $18.93 \pm 0.01$ | G-SRecec ${ }_{\text {F }}+$ SReece |
|  | 2,2'Mc | 48 to 145 | $17.50 \pm 0.43$ | $-4.11 \pm 1.20$ | $18.74 \pm 0.10$ | 41.0 | 105 | $18.90 \pm 0.05$ | $19.05 \pm 0.01$ |  |



Figure 7. Partial diagram for the conformational interconversion of 1,2-dimethylperhydropyridazine (13). ${ }^{10}$ A solid and a broken arrow represent a nonpassing and a passing N -inversion, respectively.

Since in the transition state of a nonpassing N -inversion substituents are nearly staggered as shown in Figure 1, the barrier to a nonpassing N -inversion is likely insensitive to steric factors of the substituents. In contrast, the barrier to a passing N -inversion is likely sensitive to steric factors of substituents, since the substituents are nearly eclipsed in its transition state. As stated in the Introduction, the principal cause of the barrier difference between the nonpassing N -inversion and the passing N -inversion is the electronic interaction. The barrier differences between the passing N -inversions, in which the electronic interaction operates equally, must be ascribed to the steric effects. We designate paths for the interconversion that do not involve a single-passing rotation as an inversion path. There are inversion paths that involve ring inversions. The barrier to ring inversions in cyclohexanes and piperidines seems to be insensitive to substituents on the ring and is in the range of $10-13 \mathrm{kcal} \mathrm{mol}{ }^{-1}\left(\Delta G^{\ddagger}\right) .^{22}$ This value is substantially smaller than our observed barrier values for 8 and 9. This fact cannot be explained if a ring inversion is the ratedetermining step in inversion paths. We assume, therefore, that the transition state of an inversion path lies in a passing N -inversion and that the steric interaction in the transition state is similar to that in the trans conformation involved. This means that the lowest barrier path of inversion paths should involve the trans conformation with the lowest energy. In view of the fact that the interconversion between the most stable conformations ea and ae of 1,2-dimethylperhydropyridazine (13) occurs most easily through

the less stable conformer aa rather than the more stable conformer ee (see Figure 7), ${ }^{10}$ our assumption might appear to be risky. But in the case of 13 the electronic interaction in the transition state is quite different for the two pathways: While the interconversion through aa is the nonpassing N -inversion, that through ee is the passing N -inversion. In contrast, in our case, the electronic interaction is likely approximately equal in all of the inversion paths, since they involve uniformly a passing N -inversion. Therefore, it seems reasonable to assume that the energy of the transition state parallels the steric energy of the trans conformations.

Molecular Mechanics Calculations. The potential energy of the bipiperidines is divided into the steric energy and the electronic energy. The steric energy should be similar to that of the corresponding hydrocarbons, which have $\mathrm{C}-\mathrm{H}$ bonds in place of the nitrogen lone pairs. The electronic energy largely depends upon the torsion angle of the $\mathrm{N}-\mathrm{N}$ bond. Hence, the relative stability of conformations with the same torsion angle is considered to be parallel with that of the corresponding hydrocarbons.

[^5]Table IV. Molecular Mechanics Calculation of the Corresponding Hydrocarbons for the Bipiperidine

| no. | conformation | compound ${ }^{\text {a }}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 14 |  | 15 |  | 16 |  |
|  |  | torsion angle ${ }^{\text {b }}$ | energy ${ }^{\text {c }}$ | torsion angle ${ }^{\text {b }}$ | energy ${ }^{\text {c }}$ | torsion angle ${ }^{\text {b }}$ | energy ${ }^{\text {c }}$ |
| 1 | G-SReece | -78.0 | 0.00 | -78.3 | 0.00 | -77.5 | 0.00 |
| 2 | G-SRaaee | -57.2 | 3.97 | -64.4 | 7.56 | $d$ | $d$ |
| 3 | G-SRaaa | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 4 | G-SReeaa | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 5 | G + SSeeea | 89.6 | 1.15 | 88.0 | 4.59 | $d$ | $d$ |
| 6 | $G+S S$ aea | 90.8 | 5.24 | 88.7 | 12.52 | $d$ | $d$ |
| 7 | G+SSaae | $d$ | $d$ | d | $d$ | $d$ | $d$ |
| 8 | $G+S S$ eeae | 58.3 | 3.51 | 58.0 | 3.43 | 56.7 | 3.28 |
| 9 | G-RSeaea | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 10 | G-RSacea | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 11 | G-RSacac | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 12 | G-RSeaae | $d$ | $d$ | d | $d$ | $d$ | $d$ |
| 13 | $\mathrm{G}+R \mathrm{R}$ eaee | 64.1 | 4.29 | 57.3 | 7.57 | $d$ | $d$ |
| 14 | $G+R R$ acee | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 15 | $\mathrm{G}+R R$ aeaa | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 16 | $G+R R$ eaaa | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 17 | $\mathrm{T} \pm$ SReece | -178.4 | 15.78 | -178.5 | 16.16 | $-178.5$ | 16.81 |
| 18 | $T \pm S R$ aace | -179.3 | 9.05 | -179.2 | 13.08 | $d$ | $d$ |
| 19 | $\mathrm{T} \pm$ SRaaaa | 179.9 | 4.87 | 179.9 | 12.04 | $d$ | $d$ |
| 20 | $\mathrm{T} \pm S R$ ceaa | 179.6 | 8.74 | 179.6 | 12.55 | $d$ | $d$ |
| 21 | $\mathrm{T} \pm R R$ caee | -179.0 | 8.08 | -178.8 | 11.70 | $d$ | $d$ |
| 22 | $\mathrm{T} \pm R R$ eaaa | 180.0 | 2.62 | -179.9 | 9.56 | $d$ | $d$ |
| 23 | $\mathrm{T} \pm R R$ acaa | -179.6 | 7.43 | -179.6 | 10.92 | $d$ | $d$ |
| 24 | $\mathrm{T} \pm R R$ acee | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |
| 25 | $\mathrm{T} \pm R S$ eaea | 180.0 | 1.02 | 180.0 | 7.94 | $d$ | $d$ |
| 26 | $\mathrm{T} \pm R S$ aeca | -179.6 | 5.89 | $-180.0$ | 8.94 | $d$ | $d$ |
| 27 | $\mathrm{T} \pm R$ Sacae | 180.0 | 11.05 | 180.0 | 10.88 | 180.0 | 10.16 |
| 28 | $\mathrm{T} \pm R$ Seaae | 179.9 | 5.58 | 180.0 | 8.94 | $d$ | $d$ |
| 29 | $\mathrm{T} \pm$ SSeeea | 179.1 | 7.51 | 179.0 | 11.09 | $d$ | $d$ |
| 30 | $T \pm S S$ aaea | $-180.0$ | 2.64 | 179.9 | 9.56 | $d$ | $d$ |
| 31 | $\mathrm{T} \pm$ SSaaae | 179.6 | 7.43 | 179.6 | 10.94 | $d$ | $d$ |
| 32 | $T \pm S S$ ecae | $d$ | $d$ | $d$ | $d$ | $d$ | $d$ |

${ }^{a}$ The lyydrocarbons 14,15 , and 16 correspond to the bipiperidines 7,8 , and 9 , respectively (see the text). $b$ Torsion angle $\omega$ with respect to the $\mathrm{H}-\mathrm{C} 1-\mathrm{Cl}$ '- H in degrees. $c$ Final steric energy in kilocalories per mole. The energies of the most stable conformation $\mathrm{G}-\mathrm{SR}$ eeee in each compound ( $23.48,23.86$, and $36.70 \mathrm{kcal} \mathrm{mol}^{-1}$ for 14,15 , and 16 , respectively) were set to $0.00 \mathrm{kcal} \mathrm{mol}^{-1}$. ${ }^{d}$ Sterically inipossible conformation.

We have carried out molecular mechanics calculations (MMI) ${ }^{23}$ for the corresponding hydrocarbons $1,1^{\prime}$-bi(2-methylcyclohexane) (14), 1, 1'-bi(cis-2,4-dimethylcyclohexane) (15), and 1, $1^{\prime}$-bi(cis-


$$
\begin{aligned}
& \frac{14}{14}: R=H \\
& \underline{15}: R=M e \\
& \text { 16: } R=\operatorname{tert}-B u
\end{aligned}
$$

4-tert-butyl-2-methylcyclohexane) (16) in all of the conformations depicted in Figure 5, since parameters for the $\mathrm{N}-\mathrm{N}$ bond have not been established. The results are summarized in Table IV. Based on these results, we can roughly estimate the relative stability of the conformations in the bipiperidines. Our statement that the most stable conformations in the bipiperidine are the enantiomeric gauche conformations G-SReeee and G $+S$ Reeee has been confirmed also by molecular mechanics calculation.

The Lowest Barrier Inversion Path. The most stable one of the trans conformations in 7 is $T \pm R S$ eaea. Gauche conformations that can directly arrive at $\mathrm{T} \pm R$ Seaea by a passing N -inversion are formally G $+S S$ aaea, $\mathrm{G}-R R e a a a, \mathrm{G}+R R$ eaaa, and $\mathrm{G}-S S a a e a$. The last two conformations, $G+R R$ eaaa and $G-S S a a e a$, are sterically impossible conformations. The sterically possible gauche conformation that can directly arrive at $\mathrm{G}+S S_{\text {aaea ( }} \mathrm{G}-R R$ eaaa) is $G+S$ Seeea ( $G-R R e a e e$ ), which is the next stable gauche conformation. The sterically possible gauche conformation that can arrive at $G+S$ Seeea ( $G-R R e a e e$ ) is $G+S$ Seeae ( $\mathrm{G}-R R$ aeee), which is accessible only from the most stable conformation $G$ $S$ Reeee (G-SReeee). Therefore the lowest barrier inversion path is the following: G-SReeee $\rightleftharpoons \mathrm{G}+$ SSeeae $\rightleftharpoons \mathrm{G}+$ SSeeea $\rightleftharpoons$

[^6] University, 1975, Program 318.

## $\mathrm{G}+$ SSaaea $\rightleftharpoons \mathrm{T} \pm R$ Seaea $\rightleftharpoons \mathrm{G}-R R$ eaaa $\rightleftharpoons \mathrm{G}-R$ Reaee $\rightleftharpoons \mathrm{G}-$ $R$ Raeee $\rightleftharpoons G+S R$ eeee .

The lowest barrier inversion path in 8 is the same inversion path as in 7: $\mathrm{G}-$ SReeee $\rightleftharpoons \mathrm{G}+$ SSeeae $\rightleftharpoons \mathrm{G}+$ SSeeea $\rightleftharpoons \mathrm{G}+$ SSaaea $\rightleftharpoons \mathrm{T} \pm R$ Seaea $\rightleftharpoons \mathrm{G}-R$ eaaa $\rightleftharpoons \mathrm{G}-R$ eaee $\rightleftharpoons \mathrm{G}-R R_{\text {aeee }} \rightleftharpoons$ G + SReeee.

Among the conformations that are sterically possible for 7 or 8, those with an axial methyl group are sterically prohibited in the case of 9 since in these conformations the tert-butyl group must take the axial position, which is impossible owing to the 1,3-diaxial interaction with the methyl group. As a result, for 9, there are only two sterically possible trans conformations, $\mathrm{T} \pm R S$ aeae and $\mathrm{T} \pm S R$ eeee, the former being more stable. Sterically possible gauche conformations that can arrive at $\mathrm{T} \pm R S$ aeae are $\mathrm{G}+S$ Seeae and $G-R R$ aeee. $G+S$ Seeae (G-RRaeee) is accessible only from the most stable conformation G-SReeee ( $\mathrm{G}+$ SReeee). Hence, the lowest barrier inversion path should be the following: $\mathrm{G}-S R$ eeee $\rightleftharpoons \mathrm{G}+S$ Seeae $\rightleftharpoons \mathrm{T} \pm R$ Saeae $\rightleftharpoons$ $\mathrm{G}-R$ Raeee $\rightleftharpoons \mathrm{G}+S$ Reeee.

The Lowest Barrier Rotation Path. We designate a singlepassing rotation path $\mathrm{G}-S$ Reeee $\rightleftharpoons \mathrm{T} \pm S$ Reeee $\rightleftharpoons \mathrm{G}+S$ Reeee, in which neither nitrogen inversion nor ring inversion is involved, as the pure single-passing rotation path. Energy profiles of the pure single-passing rotation path calculated by MMI for 14,15 , 16, and bi(cyclohexane) (17) are shown in Figure 8. ${ }^{24}$ The

(24) During the course of our work, Prof. E. Ösawa has obtained similar results using MM2 for cyclohexylpiperidines: Jaime, C.; Ösawa, E. J. Chem. Soc., Chem. Commun. 1983, 708; J. Chem. Soc., Perkin Trans. 2, in press.


Figure 8. Energy profiles of the bond rotation about the $\mathrm{Cl}-\mathrm{Cl}{ }^{\prime}$ bond in meso-1,1'-bi(2-methylcyclohexane) (14) (-), meso-1,1'-bi(cis-2,4dimethylcyclohexane) (15) (---), meso-1,1'-bi(cis-4-tert-butyl-2methylcyclohexane) (16) (-..-), and bi(cyclohexane) (17) (…) calculated by MMI as a function of the torsion angle $\omega\left(\mathrm{H}-\mathrm{Cl}-\mathrm{Cl}^{\prime}-\mathrm{H}\right)$. All other internal coordinates are optimized. For 14, 15, and 16, the steric energy of the most stable conformations G-SReeee and G+SReeee in each of the compounds is set to $0.00 \mathrm{kcal} \mathrm{mol}^{-1}$ (see note $c$ in Table IV). For 17 the minimum of the steric energy $\left(18.31 \mathrm{kcal} \mathrm{mol}^{-1}\right.$ at $\omega=70.0^{\circ}$ and $290.0^{\circ}$ ) is set to $0.00 \mathrm{kcal} \mathrm{mol}^{-1}$.
important features of the energy profiles are that except in the case of 17 a staggered conformation $T \pm S R$ eeee lies in the saddle point ( $15.78-16.81 \mathrm{kcal} \mathrm{mol}^{-1}$ ) and that it is ca. $6-8 \mathrm{kcal} \mathrm{mol}^{-1}$ higher than other saddle points ( $8.35-10.04 \mathrm{kcal} \mathrm{mol}^{-1}$ ), which correspond to the nearly eclipsed conformations. In Figure 8 the energy of the most stable staggered conformation is taken as the reference. It is known that MMI gives reliable steric energies for staggered conformations of hydrocarbons while it gives lower energies (ca. 10-20\% lower) for eclipsed conformations than true values. ${ }^{25}$ On the basis of this fact, the steric energies of $T \pm S$ Reeee are expected to be accurate while the steric energies of the nearly eclipsed conformations can be as large as $10.02-12.05 \mathrm{kcal} \mathrm{mol}^{-1}$, which are still lower than $\mathrm{T} \pm$ SReeee. Hence the transition state of the pure single-passing rotation path is certainly $\mathrm{T} \pm S$ Reeee. The energies of $T \pm S R e e e e$, i.e., the calculated rotational barriers ( $\Delta H^{*}$ ) for 14,15 , and 16 , are $15.78,16.16$, and $16.81 \mathrm{kcal} \mathrm{mol}^{-1}$, respectively. The experimental rotational barriers for 14,15 , and 16 are not known. Theoretical calculations of hydrazine have shown that the trans conformation is a saddle point in the $\mathrm{N}-\mathrm{N}$ bond rotation owing to the electronic interaction. ${ }^{13}$ Hence, in the bipiperidines, both the steric and the electronic effects operate to make $\mathrm{T} \pm$ SReeee a saddle point. The barriers for the pure single-passing rotation path in the bipiperidines are expected to be higher than the calculated rotational barrier for 14,15 , and 16 , since the $\mathrm{N}-\mathrm{N}$ bond is shorter than the $\mathrm{C}-\mathrm{C}$ bond and since in the bipiperidines there would be repulsive interactions between lone-pair electrons, which do not exist in the hydrocarbons. Although in our first intuition the rotational barrier in 14, 15, and 16 are the same, the calculated barriers increase in the order $\mathbf{1 4}, \mathbf{1 5}, 16$. This increase in the calculated rotational barrier can be ascribed to the increase in the rigidity of the molecules.

We designate paths for the interconversion in which nonpassing N -inversion and/or ring inversion are involved in addition to a single-passing rotation as inversion-rotation paths. Since there are impossible gauche and trans conformations, 7 and 8 have only one inversion-rotation path $\mathrm{G}-$ SReeee $\rightleftharpoons \mathrm{G}-$ SRaaee $\rightleftharpoons \mathrm{G}+-$ $R$ Reaee $\rightleftharpoons \mathrm{T} \pm R$ Reaee $\rightleftharpoons \mathrm{G}-R$ Reaee $\rightleftharpoons \mathrm{G}-R R$ aeee $\rightleftharpoons \mathrm{G}+-$ $S$ Reeee. The inversion-rotation path of 7 and 8 is, however, impossible because of the severe steric congestion at the eclipsed form (the torsion angle $\simeq 120^{\circ}$ ) between $G+R R$ eaee and $T \pm$ -
(25) Ōsawa, E.; Shirahama, H.; Matsumoto, T. J. Am. Chem. Soc. 1979, 101, 4824. Beckhause, H.-D.; Ruchardt, C.; Anderson, J. E. Tetrahedron 1982, 38, 2299. Ōsawa, E.; Musso, H. In "Topics in Stereochemistry"; Allinger, N. L., Eliel, E. L., Eds.; Wiley-Interscience: New York, 1982; Vol. 13, p 117 and references therein.

Table V. Comparison of the Observed Barriers of the
Bipiperidines ( $\Delta H^{\ddagger}$ obsd) with the Calculated Rotational Barriers ( $\Delta H^{\ddagger}$ calcd) and the Calculated Steric Energies (SE) of the Trans Conformations Involved in the Inversion Paths in the Corresponding Hydrocarbons

| bipiperidines |  |  | hydrocarbons |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| compd | $\Delta H^{\ddagger}{ }_{\text {obsd }}{ }^{a, b}$ |  | compd | $\Delta H^{\ddagger}{ }_{\text {calcd }}{ }^{a, c}$ | $\mathrm{SE}^{a, d}$ |
| 7 | 11.80 |  | $\mathbf{1 4}$ | 15.78 | 1.02 (T $\pm R S$ eaea) |
| 8 | 17.14 |  | $\mathbf{1 5}$ | 16.16 | 7.94 (T $\pm R S$ eaea) |
| 9 | 17.63 | 16 | 16.81 | 10.16 (T $\pm R S$ aeae) |  |

${ }^{a}$ kcal mol ${ }^{-\frac{1}{2}}$. ${ }^{b}$ From Table III. ${ }^{c}$ From Figure 8. ${ }^{d}$ From Table IV.
$R$ Reaee in the single-passing rotation, which is easily noticed by the inspection of models. For 9, there is no inversion-rotation path.

Hence, the pure single-passing rotation path is the lowest barrier rotation path.

The Inversion Path vs. the Pure Single-Passing Rotation Path. The above discussion has shown that the lowest barrier path for the interconversion between $G-S$ Reeee and $G+S$ Reeee in each of the bipiperidines is one of two paths, the inversion path or the pure single-passing rotation path. In Table $V$ the observed barriers of the bipiperidines are compared with the calculated steric energies of the trans conformations involved in the inversion paths and the calculated rotational barriers in the corresponding hydrocarbons. Since the observed barrier for $7\left(\Delta H^{\ddagger}=11.8 \mathrm{kcal}\right.$ $\mathrm{mol}^{-1}$ ) is substantially lower than the calculated barrier to the single-passing rotation path for $14\left(\Delta H^{*}=15.78 \mathrm{kcal} \mathrm{mol}^{-1}\right)$, the lowest barrier path in 7 is not the rotation path but the inversion path $G-S R$ eeee $\rightleftharpoons G+S$ Seeae $\rightleftharpoons G+S$ Seeea $\rightleftharpoons G+S$ Saaea $\rightleftharpoons$ $\mathrm{T} \pm R$ Seaea $\rightleftharpoons \mathrm{G}-R$ eaaa $\rightleftharpoons \mathrm{G}-R$ Reaee $\rightleftharpoons \mathrm{G}-R R$ aeee $\rightleftharpoons \mathrm{G}+$ $S$ Reeee. Hence the observed barrier is assigned to the passing N -inversion between $G+S S$ aaea and $T \pm R S$ eaea and between $G-R R e a a a$ and $T \pm R S$ eaea.

The difference between the observed barriers of 8 and 9 is much closer to the difference between the calculated rotational barriers of the corresponding hydrocarbons, 15 and 16 , than to the calculated energy difference between $T \pm R S$ eaea of 15 and $T \pm$ $R$ Saeae of 16. Moreover, the observed barriers of 8 and 9 are slightly higher than the calculated rotational barriers of 15 and 16. Therefore, we assign the observed barriers of 8 and 9 to the pure single-passing rotation path $G-S R$ eeee $\rightleftharpoons \mathrm{T} \pm$ SReeee $\rightleftharpoons$ $G+S R$ eeee. These barriers can be explained by the steric compression that involves a 1,3-diaxial-like interaction between the 2-methyl ( $2^{\prime}$-methyl) group and the equatorial $\mathrm{C}^{\prime}-\mathrm{H}(\mathrm{C} 6-\mathrm{H})$ across the $\mathbf{N} 1-N l^{\prime}$ bond. In fact, the energy profile of 17 , which does not have such a steric compression in the trans conformation, shows a minimum with $0.96 \mathrm{kcal} \mathrm{mol}^{-1}$ at $\omega=180.0^{\circ}$ and saddle points with $2.85 \mathrm{kcal} \mathrm{mol}^{-1}$ at $\omega=120.0^{\circ}$ and $240.0^{\circ}$ (see Figure 8). ${ }^{24}$ The observed barrier for 8 and 9 are well compared with the rotational barrier ( $\Delta G^{*}=17.4 \mathrm{kcal} \mathrm{mol}^{-1}$ at $-35^{\circ} \mathrm{C}$ ) of 2,2'-dimethylbiphenyl. ${ }^{26}$

The Lower Temperature Process in 7. The above discussion is further supported by the observation of the lower temperature process in 7. At lower temperatures all of the peaks of 7 further split into two peaks with intensity ratio of about 85:15. At -117 ${ }^{\circ} \mathrm{C}$ one of the methyl signals splits to a large extent $(\Delta \nu=209.5$ Hz ) with the weaker peak appearing at higher field ( $\delta 11.9$ ). The weak peak was unequivocally assigned to the axial methyl group from its $\delta$ value ${ }^{27}$ (see Table II and Figure 3). These results strongly suggest that at the lower temperature the interconversions between $G-S R$ eeee and $G+S$ Seeea via $G+S S$ eeae and between $G+S R$ eeee and $G-R R$ eaee via $G-R$ Raeee are frozen out. From the ratio of the integrated intensities of the axial and the equatorial methyl signals, the free energy of $G+S S$ eeea (as well as $G-$ $R$ Reaee) was estimated to be higher by $0.55 \mathrm{kcal} \mathrm{mol}^{-1}$ at -117 ${ }^{\circ} \mathrm{C}$ than that of $\mathrm{G}-S R e e e e$ (as well as $\mathrm{G}+\mathrm{S} R e e e e$ ). The calculated

[^7]enthalpy difference between G+SSeeea (G-RReaee) and G$S$ Reeee ( $\mathrm{G}+S$ Reeee) in 14 is $1.15 \mathrm{kcal} \mathrm{mol}^{-1}$ as shown in Table IV. The entropy contribution due to symmetry of G + SSeeea ( $\mathrm{G}-R$ Reaee) is 0 while that of $\mathrm{G}-S R$ eeee ( $\mathrm{G}+S R$ eeee) is $-R \ln$ $2(1.38 \mathrm{cal} /(\mathrm{deg} \mathrm{mol}))$, where $R$ is the gas constant. Hence, the calculated free energy difference in 14 between $G+S S$ eeea (G$R R$ eaee) and G-SReeee ( $\mathrm{G}+S$ Reeee) is $0.94 \mathrm{kcal} \mathrm{mol}^{-1}$ at -117 ${ }^{\circ} \mathrm{C}$, which is close to the observed experimental free energy difference in 7 .

In view of the fact that the barriers to the nonpassing N -inversion ( $\Delta G^{*}=7-8 \mathrm{kcal} \mathrm{mol}^{-1}$ ) in 1, 2, and $\mathbf{3}$ are lower than the barriers to the ring inversion in piperidines ( $\Delta G^{\star}=10-13 \mathrm{kcal}$ $\mathrm{mol}^{-1}$ ), it is concluded that the transition state corresponding to the observed barrier ( $\Delta G^{\ddagger}=9.2 \mathrm{kcal} \mathrm{mol}^{-1}$ at $-117^{\circ} \mathrm{C}$ ) to the interconversions of 7 between $G-S$ Reeee and G $+S$ Seeea and
 processes between G+SSeeae and G+SSeeea and between G$R$ Raeee and $\mathrm{G}-R$ Reaee, not in the nonpassing N -inversion processes between G-SRecee and G+SSeeae and between G+SReeee and G-RRaeee. In other words, it is concluded that the observed barrier is the free energy difference between the transition state of the ring-inversion processes and the most stable conformations G-SReeee and G+SReeee. In 8 and 9 the energy difference between the next most stable conformation $G+S S$ eeae ( $\mathrm{G}-$ $R R$ aeee) and the most stable conformation G-SReeee (G+$S R$ eeee) is so large that the next most stable conformation was not detected irrespective of the slowing down of the conformational interconversion at lower temperature.

## Experimental Section

${ }^{1} \mathrm{H}$ NMR ( $60-\mathrm{MHz}$ ), $90-\mathrm{MHz}{ }^{1} \mathrm{H}$ NMR, and $22.5-\mathrm{MHz}{ }^{13} \mathrm{C}$ NMR spectra were recorded on Jeol 60-HL, Varian EM-390, and Jeol FX90Q spectrometers, respectively. Mass spectra were measured on a Hitachi RMU-6D mass spectrometer. High-resolution mass spectra were measured on a Jeol D300 mass spectrometer. VPC was carried out on a Varian-Aerograph Model 920 instrument with a $20 \%$ Triton X-305 column ( $1 / 4 \mathrm{in}, \times 4 \mathrm{~m}$ ), on $60-80$ mesh Uniport B. Fractional distillation was carried out on a Perkin-Elmer NFT-51 spinning band annular still. Activated alumina powder ( 200 mesh, Wako Chemicals) was used for the column chromatography.

Materials. cis-2,4-Dimethylpiperidine (18). ${ }^{28}$ The method of Booth and Little was used for reduction of 3,5 -dimethylpyridine. ${ }^{29}$ 2,4-Dimethylpyridine ( 50 g ) was dissolved in hot dry EtOH $(800 \mathrm{~mL})$ and Na ( 85 g ) was added with magnetic stirring in small pieces at a rate sufficient to maintain boiling. The mixture was cooled, acidified with hydrochloric acid ( $30 \%$ ), and heated to remove EtOH under reduced pressure. The residue was basified with aqueous $\mathrm{NaOH}(40 \%)$, and the liberated base was extracted with ether. Distillation gave a colorless oil ( 45 g ), bp $60-67^{\circ} \mathrm{C}(6.9-7.3 \mathrm{kPa})$, shown by VPC to contain $58 \%$ of cis-2,4-dimethylpiperidine (18), $10 \%$ of the trans isomer, $7 \%$ of $1,2,3,6$ -tetrahydro-2,4-dimethylpyridine, and $24 \%$ of 1,2,5,6-tetrahydro-2,4-dimethylpyridine. The mixture ( 51.5 g ), dissolved in dilute $\mathrm{HCl}(9 \%, 253$ mL ), was hydrogenated over Adams platinum oxide catalyst ( 500 mg ) until uptake of hydrogen ceased, and the catalyst was filtered off. This procedure was repeated several times, and the filtrate was gathered. The usual method of recovery gave a mixture ( 130 g ) of cis- $(77 \%$ ) and trans(23\%) 2,4-dimethylpiperidine from 175 g of 2,4 -dimethylpyridine. Fractional distillation (reflux ratio 100 , bp $140^{\circ} \mathrm{C}$ ) gave pure $18(67 \mathrm{~g})$. Its ${ }^{1} \mathrm{H}$ NMR spectrum was identical with that reported by Wendisch et al. ${ }^{30}{ }^{13}{ }^{13} \mathrm{NMR}\left(\mathrm{CDCl}_{3}\right) \delta 52.14(\mathrm{~d}, \mathrm{C} 2), 46.96(\mathrm{t}, \mathrm{C} 6), 43.78(\mathrm{t}, \mathrm{C} 3)$, 35.02 (t, C5), 31.55 (d, C4), 23.10 (q, 2-Me), $22.60(\mathrm{q}, 4-\mathrm{Me}$ ).
meso-1,1'-Bi(cis-2,4-dimethylpiperidine) (8). A $25 \%$ aqueous solution of sodium peroxodisulfate ( $35.7 \mathrm{~g}, 150 \mathrm{mmol}$ ) was added dropwise at 0 ${ }^{\circ} \mathrm{C}$ to a stirred mixture of $18(11.3 \mathrm{~g}, 100 \mathrm{mmol})$, sodium hydroxide ( 12.0 $\mathrm{g}, 300 \mathrm{mmol}$ ), and a catalytic amount of silver nitrate ( $850 \mathrm{mg}, 5 \mathrm{mmol}$ ) in water ( 120 mL ), and the mixture was stirred for additional 3.5 h . After the saturation of the reaction mixture with sodium chloride, it was extracted with ether. The ethereal extract was dried over $\mathrm{Na}_{2} \mathrm{SO}_{4}$ and concentrated under reduced pressure. The residue was chromatographed 3 times on an alumina column with hexane as an eluant to give dl-1,1'-bi(cis-2,4-dimethylpiperidine) (19) ( 291 mg , yield $2.6 \%$ ) and meso-1, $1^{\prime}$-bi (cis-2,4-dimethylpiperidine) (8) ( 140 mg , yield $1.2 \%$ ), both

[^8]of which were colorless oils. ${ }^{13} \mathrm{C}$ NMR (THF- $d_{8} / \mathrm{CS}_{2}=5 / 6$ ) of $19 \delta$ 53.70 (d, C2, C2'), 44.19 (t, C6, C6'), 43.26 (t, C3, C3'), 35.22 (t, C5, $\mathrm{C}^{\prime}$ ), 31.77 (d, $\mathrm{C} 4, \mathrm{C4} 4^{\prime}$ ), $22.39\left(\mathrm{q}, \mathrm{CH}_{3}\right), 22.19\left(\mathrm{q}, \mathrm{CH}_{3}\right)$; mass spectrum $m / e 224\left(\mathrm{M}^{+}\right)$.

Diastereomeric mixture anal. Calcd for $\mathrm{C}_{14} \mathrm{H}_{28} \mathrm{~N}_{2}: \mathrm{C}, 74.94 ; \mathrm{H}$, 12.58; N, 12.49. Found: C, $75.20 ; \mathrm{H}, 12.46 ; \mathrm{N}, 12.34$.

4-tert-Butyl-2-methylpyridine (12). The method of Ziegler and Zeiser was used for methylation of pyridines. ${ }^{31}$ To a stirred solution of methyllithium, prepared from methyl iodide ( $142 \mathrm{~g}, 1 \mathrm{~mol}$ ) and lithium ribbon ( $17 \mathrm{~g}, 2.4 \mathrm{~mol}$ ) in ether, ${ }^{32}$ was added 4-tert-butylpyridine dropwise for 3.5 h . After 550 mL of dry toluene was added, ether was distilled off, and the solution was refluxed for 14 h . The solution was cooled with an ice bath. The generated lithium hydride and the unchanged methyllithium were decomposed by adding ice into the solution. The solution was acidified with hydrochloric acid ( 6 N ), and the separated water layer was basified with aqueous NaOH (40\%). The liberated base was extracted with ether, and the extract was dried over $\mathrm{Na}_{2} \mathrm{SO}_{4}$ and KOH . Distillation gave a colorless oil ( 102 g ) (bp 101-106 ${ }^{\circ} \mathrm{C}(5.3 \mathrm{kPa})$ ), which was shown by VPC, as well as NMR, to contain $63 \%$ of 4 -tert-butyl-2-
 tional distillation gave a mixture ( 40 g ) of $12(90 \%)$ and 4 -tert-butylpyridine ( $10 \%$ ), which was used in the catalytic hydrogenation. Preparative VPC and the subsequent distillation gave a colorless oil as an analytically pure sample of $12 .{ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) \delta 8.38(1 \mathrm{H}, \mathrm{d}, J=$ 5 Hz ), $7.2-6.8(2 \mathrm{H}, \mathrm{m}), 2.55(3 \mathrm{H}, \mathrm{s}), 1.30(9 \mathrm{H}, \mathrm{s})$; mass spectrum, $m / e 149\left(\mathrm{M}^{+}\right)$.
Anal. Caled for $\mathrm{C}_{10} \mathrm{H}_{15} \mathrm{~N}: \mathrm{C}, 80.48 ; \mathrm{H}, 10.13 ; \mathrm{N}, 9.39$. Found: C, 80.53; H, 10.18; N, 9.32 .
cis-4-tert-Butyl-2-methylpiperidine (10). Raney nickel-aluminum alloy ( $40 \%, 4 \mathrm{~g}$ ) was added slowly to a stirred aqueous solution of sodium hydroxide ( $20 \%, 100 \mathrm{~mL}$ ), which was heated at ca. $50^{\circ} \mathrm{C}$, and it was stirred for an additional 15 min at the same temperature. The supernatant layer was removed by decantation, and the nickel residue was washed with water. To the residue were added tert-butyl alcohol ( 50 mL ) and 12 ( 40 g , contained $10 \%$ of 4 -tert-butylpyridine), and the mixture was heated at $60-70^{\circ} \mathrm{C}$ for 1 h with stirring. The catalyst was filtered off, and the filtrate was placed in an autoclave. To the solution were added $\mathrm{Ru}(\mathrm{OH})_{3}(600 \mathrm{mg})^{33}$ and $\mathrm{LiOH} \cdot \mathrm{H}_{2} \mathrm{O}(100 \mathrm{mg})$, and the mixture was hydrogenated at $4053 \mathrm{kPa}, 80-120^{\circ} \mathrm{C}$. Hydrogen absorption continued for 5 h . THF ( 50 mL ) was added to the mixture, and the solution was filtered through a double layer of $\mathrm{MgSO}_{4}$ and cellulose powder. The filtrate was acidified with hydrochloric acid ( $10 \%$ ) and evaporated. The residue was basified with an aqueous solution of $\mathrm{NaOH}(20 \%)$ and was extracted with ether. The extract was dried over $\mathrm{MgSO}_{4}$, concentrated under reduced pressure, and dried again over KOH . Distillation gave 32 g of a colorless oil ( $\mathrm{bp} 92-94^{\circ} \mathrm{C}(3.7-4.0 \mathrm{kPa}$ )), which was shown by VPC, as well as NMR, to contain $85 \%$ of cis-4-tert-butyl-2-methylpiperidine ( $\mathbf{1 0}$ ), $6 \%$ of trans-4-tert-butyl-2-methylpiperidine (11), and $9 \%$ of 4-tert-butylpiperidine. The distillate was used as the material for the $\mathrm{N}-\mathrm{N}$ coupling reaction. Preparative VPC gave 10 as a colorless oil and 11 as an easily sublimable, colorless solid ( $\mathrm{mp} 59.0-60.0^{\circ} \mathrm{C}$ ).
10: ${ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) \delta 3.25-3.00(1 \mathrm{H}, \mathrm{m}), 2.75-2.35(2 \mathrm{H}, \mathrm{m})$, $1.80-1.45(3 \mathrm{H}, \mathrm{m}), 1.4-0.7(3 \mathrm{H}, \mathrm{m}), 1.07(3 \mathrm{H}, \mathrm{d}, J=6 \mathrm{~Hz}), 0.88(9$ $\mathrm{H}, \mathrm{s})$; IR (neat) $3250 \mathrm{~cm}^{-1}(\mathrm{~N}-\mathrm{H})$; mass spectrum, $m / e 155\left(\mathrm{M}^{+}\right)$.

Anal. Calcd for $\mathrm{C}_{10} \mathrm{H}_{21} \mathrm{~N}: \mathrm{C}, 77.35 ; \mathrm{H}, 13.63 ; \mathrm{N}, 9.02$. Found: C, $77.22 ; \mathrm{H}, 13.59 ; \mathrm{N}, 8.87$.

11: Mass spectrum (high resolution), $m / e 155.1679$ ( 155.1674 calcd for $\mathrm{C}_{10} \mathrm{H}_{21} \mathrm{~N}$ ); ${ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) \delta 3.58-3.18(1 \mathrm{H}, \mathrm{br} \mathrm{s}), 2.95-2.72(2$ $\mathrm{H}, \mathrm{m}), 2.70(1 \mathrm{H}, \mathrm{s}), 1.75-1.05(5 \mathrm{H}, \mathrm{m}), 1.18(3 \mathrm{H}, \mathrm{d}, J=7 \mathrm{~Hz}), 0.85$ ( $9 \mathrm{H}, \mathrm{s}$ ); IR (Nujol) $3410 \mathrm{~cm}^{-1}(\mathrm{~N}-\mathrm{H})$.
meso-1,1'-B1(cis-4-tert-butyl-2-methylpiperidine) (9). A $25 \%$ aqueous solution of sodium peroxodisulfate ( $25.0 \mathrm{~g}, 105 \mathrm{mmol}$ ) was added dropwise below $10^{\circ} \mathrm{C}$ to a stirred mixture of $\mathbf{1 0}$ (a mixture of $85 \%$ of 10 and $15 \%$ of the trans isomer $11,10.8 \mathrm{~g}, 60 \mathrm{mmol}$ ), sodium hydroxide ( 8.4 g , 210 mmol ), and a catalytic amount of silver nitrate ( $595 \mathrm{mg}, 3.5 \mathrm{mmol}$ ) in water ( 84 mL ), and the mixture was stirred for an additional 4.5 h . After the reaction mixture was saturated with sodium chloride, it was extracted with ether. The extract was dried over $\mathrm{Na}_{2} \mathrm{SO}_{4}$ and evaporated under reduced pressure. The residue was chromatographed several times on an alumina column with hexane as the eluant to give $d l-1,1^{\prime}$-bi(cis4 -tert-butyl-2-methylpiperidine) (20) ( 89 mg , yield $1 \%$ ) and the meso isomer (9) ( 40 mg , yield $0.4 \%$ ).
20: $\mathrm{mp} 121.0-122.0^{\circ} \mathrm{C}$ (needles from MeOH ); ${ }^{13} \mathrm{C}$ NMR (THF- $d_{8}$ ) $\delta 54.81$ ( $\mathrm{d}, \mathrm{C} 2, \mathrm{C} 2^{\prime}$ ), $47.68\left(\mathrm{t}, \mathrm{C} 4, \mathrm{C} 4^{\prime}\right), 44.04\left(\mathrm{t}, \mathrm{C} 6, \mathrm{C} 6^{\prime}\right), 37.21(\mathrm{t}, \mathrm{C} 3$,

[^9]$\mathrm{C}^{\prime}$ ), $32.49\left(\mathrm{~s}, \mathrm{C}\left(\mathrm{CH}_{3}\right)_{3}\right), 28.19\left(\mathrm{~d}, \mathrm{C} 5, \mathrm{C}^{\prime}\right), 27.74\left(\mathrm{q}, \mathrm{C}\left(\mathrm{CH}_{3}\right)\right), 21.45$ ( $\mathrm{q}, 2-\mathrm{CH}_{3}, 2^{\prime}-\mathrm{CH}_{3}$ ); mass spectrum, $m / e 308\left(\mathrm{M}^{+}\right)$.

Anal. Calcd for $\mathrm{C}_{20} \mathrm{H}_{40} \mathrm{~N}_{2}: \mathrm{C}, 77.85 ; \mathrm{H}, 13.07 ; \mathrm{N}, 9.08$. Found: C , 77.66; H, 12.89; N, 9.07.

9: $\mathrm{Mp} 94.0-95.0^{\circ} \mathrm{C}$ (prisms from MeOH ); mass spectrum, $m / e 308$ ( $\mathrm{M}^{+}$).

Anal. Caled for $\mathrm{C}_{20} \mathrm{H}_{40} \mathrm{~N}_{2}: \mathrm{C}, 77.85 ; \mathrm{H}, 13.07 ; \mathrm{N}, 9.08$. Found: C , 77.80; H, 12.79; N, 8.97.
${ }^{13} \mathrm{C}$ NMR Measurements. All of the variable-temperature ${ }^{13} \mathrm{C}$ NMR spectra were recorded at 22.5 MHz on a Jeol FX90Q spectrometer fitted with a variable-temperature controller Jeol NM-VTS. Typical spectrometer settings are as follows: spectral width 2000 Hz ; number of data points, 8 K ; pulse angle, $55^{\circ}$. The spectrometer was locked on a deuterium signal from THF- $d_{8}$ or diglyme- $d_{14}$. All NMR samples were freeze-thaw degassed and sealed in $10-\mathrm{mm}$ o.d. sample tubes. Temperatures were calibrated with a chromel-alumel thermocouple, which was inserted, at receiver coil height, into another $10-\mathrm{mm}$ o.d. sample tube containing an equal volume of silicone oil. The accuracy of the quoted temperatures is within $\pm 1^{\circ} \mathrm{C}$.

Line-shape calculations were performed on a Hitac M200H computer of Computer Centre University of Tokyo using the programs DNMR ${ }^{34}$ and LSQM2. The spin-spin relaxation time ( $T_{2}$ ) was replaced by an effective $T_{2}$, which was estimated from the average of the half-height line width of the $\mathrm{Me}_{4} \mathrm{Si}$ peak in the whole region of the exchange process. Errors in the enthalpy and entropy of activation are $95 \%$ confidence limits from a least-square fit of the Eyring rate equation. Error in the free energy of activation was evaluated from the error of enthalpy and entropy of activation by using the equation of Binsch and Kessler. ${ }^{35}$

In the $T_{c}$ method, we obtained the free energy of activation at the coalescence temperature from the following equation ${ }^{21}$

$$
\begin{equation*}
\Delta G^{*}=R T_{\mathrm{c}}\left[\ln \left(\frac{(2 R)^{1 / 2}}{\pi N h}\right)+\ln \left(\frac{T_{\mathrm{c}}}{\Delta \nu}\right)\right] \tag{2}
\end{equation*}
$$

where $R$ is gas constant, $T_{\mathrm{c}}$ the coalescence temperature, $N$ Avogadro constant, and $h$ Planck constant. Errors in $\Delta G^{*}{ }_{c}\left(\sigma_{G}\right)$ were calculated by applying the well-known equation for the propagation of errors ${ }^{36}$ to eq 2

$$
\begin{aligned}
\sigma_{\mathrm{G}}\left(\mathrm{~J} \mathrm{~mol}^{-1}\right) & =\left[\left(\frac{\partial\left(\Delta G_{\mathrm{c}}^{*}\right)}{\partial T_{\mathrm{c}}}\right)^{2} \sigma_{T}^{2}+\left(\frac{\partial\left(\Delta G_{\mathrm{c}} \mathrm{c}\right)}{\partial(\Delta \nu)}\right)^{2} \sigma_{\Delta \nu}^{2}\right]^{1 / 2} \\
& =8.3144\left[\left[23.96+\ln \left(T_{\mathrm{c}} / \Delta \nu\right)\right]^{2} \sigma_{T}^{2}+\left(T_{\mathrm{c}} / \Delta \nu\right)^{2} \sigma_{\Delta \nu}{ }^{2}\right]^{1 / 2}
\end{aligned}
$$

where $\sigma_{T}$ is the mean error of $T_{c}$ in kelvin and $\sigma_{\Delta \nu}$ is the mean error of $\Delta \nu$ in hertz.

The free energy difference between G-SReeee and G+SSeeea (or $\mathrm{G}+S$ Reeee $\rightleftharpoons \mathrm{G}-R R$ eaee) in 7 was determined from the equilibrium constant, which was estimated from the peak area ratio of the split peaks of $C 6^{\prime}$. It was obtained by cutting and weighing the appropriate portion of the recorded spectra.

Assignment of ${ }^{13} \mathrm{C}$ NMR Signals of 7, 8, and 9. Assignment of the signals in the high-temperature spectra of 7,8, and 9 was made on the basis of the off-resonance spectra and of the similarity between the chemical shifts of the parent piperidine and that of the corresponding 1,1'-bipiperidine.

The assignment of the signals in the high-temperature spectra makes possible the grouping of corresponding resonances at low temperature. Assignment of signals for 7 in the low-temperature (at $-117^{\circ} \mathrm{C}$ ) spectrum rests on comparison of the experimental chemical shifts with calculated ones (Table II), which were obtained by the following procedure: (i) Chemical shifts for the corresponding hydrocarbon 14 in an appropriate conformation were calculated from the parameters of Dalling and Grant, which were derived from perhydroanthracenes and perhydrophenanthrenes, ${ }^{37}$ since the ${ }^{13} \mathrm{C}$ chemical shift data of 14 were not available in the literature. (ii) The effects caused by the replacement of two $\mathrm{C}-\mathrm{H}$ groups by nitrogen atoms were added to the calculated chemical shifts for 14. We assume that the chemical shift change caused by the replacement of the CH groups by nitrogen atoms in 14 is equal to that caused by the replacement of the $\mathrm{CH}_{2}$ group by NH in cyclohexane; thus, the chemical shift change of carbon atoms $\alpha, \beta$, and $\gamma$ to the replacement center is $21.4,1.2$, and -0.6 ppm , respectively. ${ }^{17}$
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The following example illustrates the procedure for the signal of C 2 in conformation G-SReeee. In the analogous conformation of 14 the tertiary C2 carbon ( $T$ ) has three carbons in $\alpha$ and also three carbons in $\beta$ position, C 2 is involved in three $V_{8}$ interactions (C3-C2-C1-C6, 2-$\mathrm{Me}-\mathrm{C} 2-\mathrm{Cl}-\mathrm{Cl}^{\prime}, \mathrm{C} 4-\mathrm{C} 3-\mathrm{C} 2-\mathrm{C} 1$ ) and in two $V_{\mathrm{t}}$ interactions (C3-C2$\mathrm{C} 1-\mathrm{Cl}^{\prime}, 2-\mathrm{Me}-\mathrm{C} 2-\mathrm{Cl}-\mathrm{C} 6$ ), and the proton attached to C 2 is interacting with one of the $\mathrm{C} 6^{\prime}$ protons ( $\gamma_{\mathrm{HH}}$ ). Hence the predicted chemical shift of the hydrocarbon $\delta_{\mathrm{BC}}(\mathrm{C} 2)$ is given by

$$
\delta_{\mathrm{BC}}(\mathrm{C} 2)=-2.49+3 \alpha+3 \beta+T+3 V_{\mathrm{B}}+2 V_{\mathrm{t}}+\gamma_{\mathrm{HH}}=33.84
$$

By adding the effect of the $\mathrm{CH}-\mathrm{N}$ replacement, we obtain the chemical shift of C 2 of $7 \delta_{\mathrm{BP}}(\mathrm{C} 2)$ :

$$
\delta_{\mathrm{BP}}(\mathrm{C} 2)=33.84+21.4+1.2=56.44
$$

In a similar fashion, all of the signals for the ring carbons of G $S$ Reeee and $G+S S$ eeea were calculated. In this calculation it is assumed that the effect of a lone pair is equal to that of a $\mathrm{C}-\mathrm{H}$ bond in $\gamma$-gauche steric interactions. Although this seems to be a poor assumption, the magnitude of the interaction between $\gamma$-gauche hydrogens ( $\gamma_{\mathrm{HH}}$ ), which is one of the significant steric interactions, has been proved to be nearly equal to that of the $\gamma$-gauche hydrogen and a lone-pair interaction by the examination of the literature data; ${ }^{10}$ the chemical shift difference between the 6 -axial- $\mathrm{CH}_{3}$ of 1,2,3,6-tetramethylperhydropyridazine in the conformation 21 ( $\delta 18.74$ ) and that for the 1 -axial- $\mathrm{CH}_{3}$ of 1,2,3,4-tetra-


21

$\underline{22}$
methylcyclohexane in the analogous conformation 22 ( $\delta$ 18.82), which was calculated from the parameters of Dalling and Grant, is negligibly small (0.08) ${ }^{38}$ On the basis of the comparison of the calculated with the observed chemical shifts, assignment of the signals for $\mathrm{C} 2, \mathrm{C} 2^{\prime}, \mathrm{C} 6$, and $\mathrm{C}^{\prime}$ was reliably performed, but the differentiation between the signals for C 3 and $\mathrm{C} 3^{\prime}, \mathrm{C} 4$ and $\mathrm{C} 4^{\prime}$, or C 5 and $\mathrm{C} 5^{\prime}$ was unsuccessful since the calculation gives equal values for each set. The assignment of $2-\mathrm{CH}_{3}$ and $2^{\prime}-\mathrm{CH}_{3}$ was made considering the $\gamma$-gauche steric interaction.

Assignment of the signals in the low-temperature spectra of 8 was performed in a similar fashion except in the case of the peaks for C 2 and C6, in which the two peaks were so close that they were not differentiated by the inspection of the signal splitting process in the course of temperature variation but clearly differentiated by the measurement of $T_{1} ; T_{1}$ of $C^{\prime}, \mathrm{C} 2, \mathrm{C} 6$, and $\mathrm{C}^{\prime}$ were $2.0,1.8,1.2$, and 1.2 s , respectively. Assignment of the four peaks for methyl groups in the low-temperature spectrum was made on the basis of the temperature dependence of chemical shifts. Considering steric effects, the larger splitting set was assigned to $2,2^{\prime}-\mathrm{CH}_{3}$ and the smaller splitting set was assigned to $4,4^{\prime}$ $\mathrm{CH}_{3}$. Thus, assignment of the methyl peaks in the high-temperature spectrum was also accomplished.

In the case of 9 , assignment of the peaks for C 2 and C 6 in the lowtemperature spectrum was similarly made on the basis of the $T_{1}$ measurements.

Molecular Mechanics Calculations. Molecular mechanics calculations were carried out with Allinger's MM1 program, ${ }^{23}$ which was partially modified by the Ōsawa, Kureha group and us without changing the parameters for the force field, on a Hitac M 280 H of Computer Centre University of Tokyo. In the calculation of each of the gauche conformations in 14, 15, and 16 (Table IV), the full-relaxation technique was used, and all structures were optimized without symmetry constraints. The steric energies of the trans conformations (Table IV) and the energy profiles for the rotation about the $\mathrm{Cl}-\mathrm{Cl}^{\prime}$ bond of $14,15,16$, and 17 were calculated by using the Wiberg-Boyd bond drive technique. ${ }^{39}$

Acknowledgment. We greatly acknowledge Professor E. Ōsawa of Hokkaido University for offering the program for molecular mechanics calculation MMI and for informing us of his latest results with valuable suggestions. We also thank Dr. A. Tomonaga, Dr. K. Kasai, and Dr. H. Chuman of Kureha Chemical Ind. Co., Ltd., for offering the program ZMMIP for generating coordinate data and the molecular mechanics program MMI and Dr. A. Itai of our university for her help in the use of mmi on a Hitac M-280H computer of Computer Centre University of Tokyo. We are deeply
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and The Ministry of Education for the purchase of a Jeol-FX90Q spectrometer. We are also indebted to the referees for valuable suggestions.

Registry No. 7, 78705-55-2; 8, 78705-56-3; 9, 80639-04-9; 10, 72036-76-1; 11, 72036-78-3; 14, 62859-46-5; 15, 88131-16-2; 16, 88131-17-3; 17, 92-51-3.

# The Microwave Spectrum, Structure, and Electric Dipole Moment of 1,2,4-Trithiolane 

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#### Abstract

The rotational spectra of eight isotopic species of 1,2,4-trithiolane (the sulfur analogue of ethylene ozonide) were assigned and a structure determined by least-squares fitting of the moments of inertia. The molecule has a disulfide-twist half-chair conformation with $C_{2}$ symmetry. The structural parameters for the ring atoms are the following: $r(S-S)=2.044$ (2) $\AA, r\left(\mathrm{C}-\mathrm{S}_{\mathrm{s}}\right)=1.829$ (2) $\AA, r\left(\mathrm{C}-\mathrm{S}_{\mathrm{d}}\right)=1.808$ (2) $\AA, \angle \mathrm{C}-\mathrm{S}-\mathrm{S}=93.8(1)^{\circ}, \angle \mathrm{C}-\mathrm{S}-\mathrm{C}=99.4(1)^{\circ}, \angle \mathrm{S}-\mathrm{C}-\mathrm{S}=110.0(1)^{\circ}$, $\tau(\mathrm{C}-\mathrm{S}-\mathrm{S}-\mathrm{C})=52.8(3)^{\circ}, \tau(\mathrm{S}-\mathrm{S}-\mathrm{C}-\mathrm{S})=46.4(4)^{\circ}$, and $\tau(\mathrm{C}-\mathrm{S}-\mathrm{C}-\mathrm{S})=20.2(1.0)^{\circ}$. Vibrational satellites $(v=1-4)$ from an antisymmetric mode with a fundamental frequency of $82 \pm 10 \mathrm{~cm}^{-1}$ were observed. A dipole moment of 0.465 (4) D was determined. No effects of fluxional behavior were observed since all the measurements were on vibrational states considerably below the estimated barrier to pseudorotation of $3-6 \mathrm{kcal} \mathrm{mol}^{-1}$.


The structure and conformational properties of disulfides and cyclic disulfides have attracted interest because of the bearing they have on the structure of cystine residues in proteins. Scheraga and co-workers ${ }^{1}$ have used vibrational and crystallographic data along with theoretical calculations to obtain insight on changes in properties when the dihedral angle, $\tau(\mathrm{CS}-\mathrm{SC})$, is varied. Bock and co-workers have investigated the correlation between the photoelectron spectra and dihedral angle ${ }^{2}$ and provided an especially extensive study of the fluxionality properties of 1,2 -dithiolane ${ }^{2 c}\left(\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{S}-\mathrm{S}\right)$ and its radical cation using photoelectron spectroscopy (PES), electron-spin resonance, and ab initio calculations. On the other hand, there has been little gas-phase structural data from microwave (MW) or electrondiffraction studies of cyclic disulfides.

As an outgrowth of our interest in ozonide structures, we undertook a MW study of 1,2,4-trithiolane, $\mathrm{CH}_{2}-\mathrm{S}-\mathrm{S}-\mathrm{CH}_{2}-\mathrm{S}$ (sometimes called trithio ozonide), which is the sulfur analogue of ethylene ozonide and the prototype species in the 1,2,4-trithiolane series. Until Morita and Kobayashi ${ }^{3}$ provided a reliable synthesis and several bona fide properties in 1967, there was little previous discussion of it in the literature. ${ }^{4}$ On the basis of its vibrational and PES spectra, ${ }^{5} C_{2}$ symmetry has been deduced and
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a CS-SC dihedral angle of about $50^{\circ}$ was estimated. Molecular mechanics calculations ${ }^{6}$ have also indicated a twisted conformer with a dihedral angle of about $46^{\circ}$ while a flexible conformation and a low barrier to pseudorotation ( $56 \mathrm{kcal} \mathrm{mol}^{-1}$ ) have been inferred from its proton NMR spectrum ${ }^{7}$ which remains a singlet at temperatures down to $-117^{\circ} \mathrm{C}$.

More detailed structures are available for three substituted 1,2,4-trithiolanes containing exo-carbon double bonds. ${ }^{8-10}$ Species

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